

# Variable-frequency EPR study of $\text{Mn}^{2+}$ -doped $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$ single crystal at 9.6, 36, and 249.9 GHz: structural phase transition

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## Abstract

Multifrequency electron paramagnetic resonance studies on the  $\text{Mn}^{2+}$  impurity ion in a mixed single crystal  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  were carried out at 9.62 (X-band) in the range 120–295 K, at 35.87 (Q-band) at 77 and 295 K, and at 249.9 GHz (far-infrared band) at 253 K. The high-field EPR spectra at 249.9 GHz are well into the high-field limit leading to a considerable simplification of the spectra and their interpretation. Three magnetically inequivalent, but physically equivalent,  $\text{Mn}^{2+}$  ions with their respective magnetic *Z*-axes oriented along the crystallographic [1 0 0], [0 1 0], [0 0 1] axes were observed. Simultaneous fitting of EPR line positions observed at X-, Q-, and far infra-red bands was performed using a least-squares procedure and matrix diagonalization to estimate accurately the  $\text{Mn}^{2+}$  spin-Hamiltonian parameters. The temperature variation of the linewidth and peak-to-peak intensities of the EPR lines indicate the presence of  $\lambda$ -transitions in the mixed  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal at 242 and 228 K consistent with those observed in the pure  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals, respectively. A superposition-model analysis of the spin-Hamiltonian parameters reveals that the local environment of the  $\text{Mn}^{2+}$  ion is considerably reorganized to produce axially symmetric crystal fields about the respective *Z*-axes of the three magnetically inequivalent ions as a consequence of the vacancy created due to charge-compensation when the divalent  $\text{Mn}^{2+}$  ion substitutes for a monovalent  $\text{NH}_4^+$  ion in the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal. This reorganization is almost the same as that observed in  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  single crystals, although the latter two are characterized by different, simple cubic and face-centered cubic, structures.

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## 1. Introduction

Ammonium halides, which possess cubic crystal structures, are attractive materials for studying a variety of different structural phase transitions associated with ferroelectric or antiferroelectric ordering of the ammonium ions. The ferroelectric behavior of the mixed bromide–chloride  $\text{NH}_4\text{Cl}_{1-x}\text{Br}_x$  compounds was observed to differ from that of either the pure  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{Br}$  compounds [1]. Electron paramagnetic resonance (EPR) studies of heterovalent transition metal ions doped in alkali and ammonium halides are interesting because they provide an opportunity to study

various sites available for occupation by impurity paramagnetic ions in the host materials, associated charge-compensating mechanisms, and the resulting environment in the vicinity of the probe impurity EPR ion. The EPR of  $\text{Mn}^{2+}$ -doped  $\text{NH}_4\text{Cl}$  has been reported by several groups [2–11]. The nature of the site occupied by the  $\text{Mn}^{2+}$  ion has been controversial. Abe and Shirai [2] first reported values of the parameters *D*, *A*, and *g* from their EPR investigations of the  $\text{Mn}^{2+}$  ion in  $\text{NH}_4\text{Cl}$  crystal. Zaripov and Chirkin [3,4] obtained more precise values of these parameters from their temperature-dependent EPR investigations at 37 and 55 GHz, and determined the negative sign of the parameter *D* from their low-temperature experiment. X-band EPR studies of Forman and van Wyk on  $\text{Mn}^{2+}$ -doped  $\text{NH}_4\text{Cl}$  [5,6] led to the observation of a complex EPR spectrum, due to the microwave quantum (X-band, 9.5 GHz) used

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being very close to one of the two electronic zero-field splittings (ZFS  $\sim 9$  GHz). They concluded that when the divalent  $\text{Mn}^{2+}$  ion replaces the monovalent  $\text{NH}_4^+$  ion in  $\text{NH}_4\text{Cl}$ , charge-compensation occurs by creation of a vacancy at the nearest-neighbor cation position in the vicinity of the manganese ion. Seed [7] suggested a different charge-compensation configuration from his study of  $\text{Mn}^{2+}$  EPR spectra, in which the  $\text{Mn}^{2+}$  ion was situated interstitially between two  $\text{H}_2\text{O}$  molecules on the boundary of two unit cells, substituting for an  $\text{NH}_4^+$  ion. The appearance of numerous forbidden hyperfine EPR lines at X-band was investigated in detail by Lupei et al. [8]. Bramley and Strach [9] reported improved values of  $\text{Mn}^{2+}$  EPR parameters in  $\text{NH}_4\text{Cl}$ . Kennewell et al. [10] found only a small change in the value of the  $D$  parameter and no marked anomaly in the  $A$  parameter for the  $\text{Mn}^{2+}$  ion upon passing through the transition temperature near the  $\lambda$ -transition ( $T_\lambda = 242$  K) in an  $\text{NH}_4\text{Cl}$  crystal. Van Wyk [11] found a small peak in the EPR linewidth near  $T_\lambda$ .

EPR spectra of the  $\text{Mn}^{2+}$  ion in  $\text{NH}_4\text{I}$  single crystal were first investigated by Chand et al. [12–14] at X- and Q-bands. Later, the temperature dependence of the EPR spectrum of the  $\text{Mn}^{2+}$  ion through two phase transitions, at 256 and 231 K, in  $\text{NH}_4\text{I}$  was reported by Chand [15], who found pronounced changes in the EPR spectrum, increasing EPR linewidth and decreasing peak-to-peak intensity near 256 K, as well as a much weaker effect at 231 K.

Alternative charge-compensation models [4,7,10] in  $\text{Mn}^{2+}$ -doped alkali halides crystals grown from aqueous solutions have also been proposed. In this model, the  $\text{Mn}^{2+}$  ion is associated with  $\text{H}_2\text{O}$  impurity molecules, which occupy the two nearest  $\text{NH}_4^+$  positions on the same cubic axis. However, it was pointed out that this model was not valid [13,15] because heat treatment could easily affect EPR spectra in this case, concluding that charge-compensation occurs due to a vacancy in nearest-neighbor cation positions.

The  $\text{Mn}^{2+}$  ion doped in ammonium halide single crystals, e.g.,  $\text{NH}_4\text{Cl}$ ,  $\text{NH}_4\text{I}$ , is characterized by unusually large zero-field splittings (ZFS) for inorganic crystals [16] ( $b_2^0 = D = -4.498$  GHz and  $-4.515$  GHz for  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$ , respectively, at room temperature) resulting in complex EPR spectra at X-band due to the microwave frequency not being sufficiently large compared to the ZFS. On the other hand, in the  $\text{NH}_4\text{Br}$  crystal in the tetragonal phase, Sastry [17] observed the  $\text{Mn}^{2+}$   $D$  value to be quite small ( $\sim 1.51$  GHz) compared to that in  $\text{NH}_4\text{Cl}$ , and concluded that in this crystal  $\text{Mn}^{2+}$  enters substitutionally for  $\text{NH}_4^+$  with the charge-compensating vacancy being far removed from the  $\text{Mn}^{2+}$  ion.

EPR at high frequencies can lead to a considerable simplification of spectra with a large ZFS. In favorable cases the value of  $D$  can be directly estimated from the

spectrum [18,19]. This greatly simplifies the spectral analysis. It is the purpose of this paper to report a multifrequency EPR study of the mixed crystal  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  doped with  $\text{Mn}^{2+}$ . Since the  $\text{Cl}^-$  and  $\text{I}^-$  ions possess different electronegativities, as well as different nuclear spins, their interactions may modify spin-Hamiltonian parameters in the mixed crystal  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  from those in the pure crystals. Further, both  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  single crystals exhibit structural phase transitions with decreasing temperature, from the  $\text{Fm}3\text{m}$  space symmetry group to the  $\text{Pm}3\text{m}$  space symmetry group, at 457 and at 256 K, respectively, as well as  $\lambda$ -transitions, at 242 and 231 K, respectively. Therefore, the mixed  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal is also expected to exhibit similar structural phase transitions in this temperature range, which may be detected by EPR. The frequencies used in the study presented here are X-band (9.6 GHz), Q-band (35.87 GHz), and far-infrared (FIR) band (249.9 GHz). A multifrequency approach, fitting all EPR line positions observed at various frequencies simultaneously, enables one to estimate the SHP more precisely: the  $g$  values and ZFS parameters are determined more accurately at higher frequencies, while the hyperfine-structure (HF) parameters are determined more accurately at low frequencies [16,18].

## 2. Crystal growth and structure

Single crystals of the mixed compound  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  doped with  $\text{Mn}^{2+}$  were grown by slow evaporation of a stoichiometrically saturated aqueous solution to which  $\sim 0.1$  wt%  $\text{MnCl}_2$  was added. To prevent dendritic growth,  $\sim 2$  wt% urea was added as growth modifier. The crystals were grown in the dark at 300 K to avoid photo-dissociation of ammonium iodide. Beautiful colorless cubic-shaped crystals of optical quality were obtained. The composition was verified by chemical analysis, while the single-crystal quality was checked by X-rays. The crystals possessed the SC (simple cubic: CsCl structure) of pure  $\text{NH}_4\text{Cl}$  at 300 K, and were characterized by perfect  $\{100\}$  cleavage planes.

The space group of  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  are  $\text{O}_h^1$  ( $\text{Pm}3\text{m}$ ) and  $\text{O}_h^5$  ( $\text{Fm}3\text{m}$ ) below and above their respective transition temperature ( $T_c$ ); for  $\text{NH}_4\text{Cl}$  (CsCl: SC structure)  $T_c = 457$  K [20] and for  $\text{NH}_4\text{I}$  (NaCl: FCC structure)  $T_c = 256$  K [21]. The point group at the site of  $\text{NH}_4^+$  ions is  $\text{O}_h$  for both crystals.  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals undergo  $\lambda$ -transition from cubic  $\text{O}_h^1$  (CsCl structure) to tetragonal  $D_{4h}^7$  space group ( $\text{PH}_4\text{I}$  structure) at 242 and 231 K, respectively. Since  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals possess different cubic structures, there are several sites available for substitution of the  $\text{I}^-$  ion in the  $\text{NH}_4\text{Cl}$  lattice, as well as different configurations for the charge-compensation states in the resulting mixed compound  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$ . The SC cubic structure with the positions

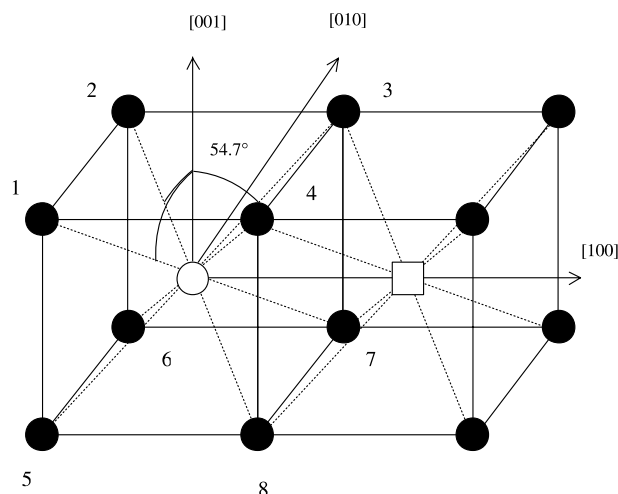


Fig. 1. The structure of the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal, showing the impurity ion  $\text{Mn}^{2+}$ , and the vacancy created due to charge-compensation and the ligand halide ions. Open circles are the cations  $\text{NH}_4^+$ , substituted for by the  $\text{Mn}^{2+}$  ion; black circles are the anions  $\text{Cl}^-$  or  $\text{I}^-$ ; and square indicates a vacancy for charge-compensation. Similar vacancies are expected adjacent to the  $\text{Mn}^{2+}$  ion in the  $[100]$ ,  $[\bar{1}00]$ ,  $[010]$ ,  $[0\bar{1}0]$ ,  $[001]$ ,  $[00\bar{1}]$  directions.

of the various ions and possible vacancy site for charge-compensation due to substitution of a divalent  $\text{Mn}^{2+}$  ion at the site of a monovalent  $\text{NH}_4^+$  ion in  $\text{NH}_4\text{Cl}$  is shown in Fig. 1.

### 3. EPR spectra and their interpretation: phase transition and spin-Hamiltonian parameters (SHP)

#### 3.1. Experimental arrangement

EPR measurements at 249.9 GHz were carried out at 253 K at Cornell University on a spectrometer that uses a transmission Fabry–Pérot cavity in the warm bore of a superconducting magnet dewar with an ambient temperature of 253 K. The magnetic field can be varied from 0.0 to 9.3 T, the field modulation being 0.1–0.5 mT at approximately 100 kHz. General experimental details of the 249.9-GHz spectrometer can be found in [22]. In particular, the use of an In-Sb hot electron bolometer improved the  $S/N$  ratio by a factor of 5–10 [18]. The X- and Q-band measurements were made on Bruker and Varian spectrometers, respectively, at Concordia University; the former was equipped with an Bruker liquid-nitrogen accessory for temperature variation in the range 120–295 K, while the latter used a liquid nitrogen dewar for measurements at 77 K. The magnetic field was limited to 1.3 T at Q-band. The X-band measurements were carried out at room (295 K), liquid nitrogen (125 K), and in the temperature range 120–300 K, while those at Q-band were done at 295 and 77 K.

#### 3.2. EPR spectra

The  $\text{Mn}^{2+}$  EPR spectra in the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal at 9.62 GHz (295 K), 35.87 GHz (295 K), and 249.9 GHz (253 K) are exhibited in Fig. 2 for rotation of the external magnetic field  $\mathbf{B}$  in the plane perpendicular to a cubic edge of the crystal. The VHF (249.9 GHz) spectra readily indicate the presence of three magnetically inequivalent, but physically equivalent,  $\text{Mn}^{2+}$  ions in the crystal with the respective magnetic Z-axes being oriented along the crystallographic axes,  $[100]$ ,  $[010]$ ,  $[001]$ . Thus, the Z-axis of one ion and the X- and Y-axes of the two other ions are found to be coincident. Furthermore, the EPR spectra for each of the three magnetically inequivalent  $\text{Mn}^{2+}$  ions about its magnetic Z-axis showed axial symmetry, so that the spectra for  $B||X$  and  $Y$ -axes are the same. Each fine-structure (FS) line splits into six hyperfine (HF) lines as the  $^{55}\text{Mn}$  nucleus (100% natural abundance) possesses nuclear spin  $I = 5/2$  ( $g_n = 1.382$ ). As seen from Fig. 2 it is relatively difficult to identify the lines belonging to the three magnetically inequivalent ions at X- and Q-bands. The angular variations of  $\text{Mn}^{2+}$  spectra were also recorded at lower temperatures: at 77 K (36.06 GHz) and at 125 K (9.69 GHz).

#### 3.3. Temperature variation of EPR spectrum: phase transition

The temperature variation of the X-band EPR spectrum is expected to show changes in the  $\text{Mn}^{2+}$  EPR spectrum in  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal, which are expected to be consistent with the  $\lambda$ -transitions at 241 and 231 K occurring, respectively, in the pure  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals. The behavior of the widths and peak-to-peak intensities of the  $\text{Mn}^{2+}$  EPR hyperfine lines in the highest-field sextet for intermediate orientations of the external magnetic field, as shown in Fig. 3, clearly demonstrates the occurrence of the corresponding  $\lambda$ -transitions in the mixed crystal  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  at  $245 \pm 2$  and 228–232 K. The transition at 228–232 K has a significantly weaker effect on the spectrum than that at 245 K and is spread out over an interval of 4 K, as indicated by the intensity and width of lines, presumably because of the much lower concentration of  $\text{I}^-$  ions (10%) as compared to that of  $\text{Cl}^-$  ions (90%) in the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal. Changes in the peak-to-peak intensity in the range 228–232 K occurred for other orientations of the magnetic field  $\mathbf{B}$  as well.

#### 3.4. Spin-Hamiltonian parameters (SHP)

The three magnetically inequivalent, but physically equivalent, ions are described by the same set of SHP. The EPR line positions for a magnetically inequivalent  $\text{Mn}^{2+}$  ion were fitted to the spin Hamiltonian (SH) appropriate to axial site symmetry [19,23]:

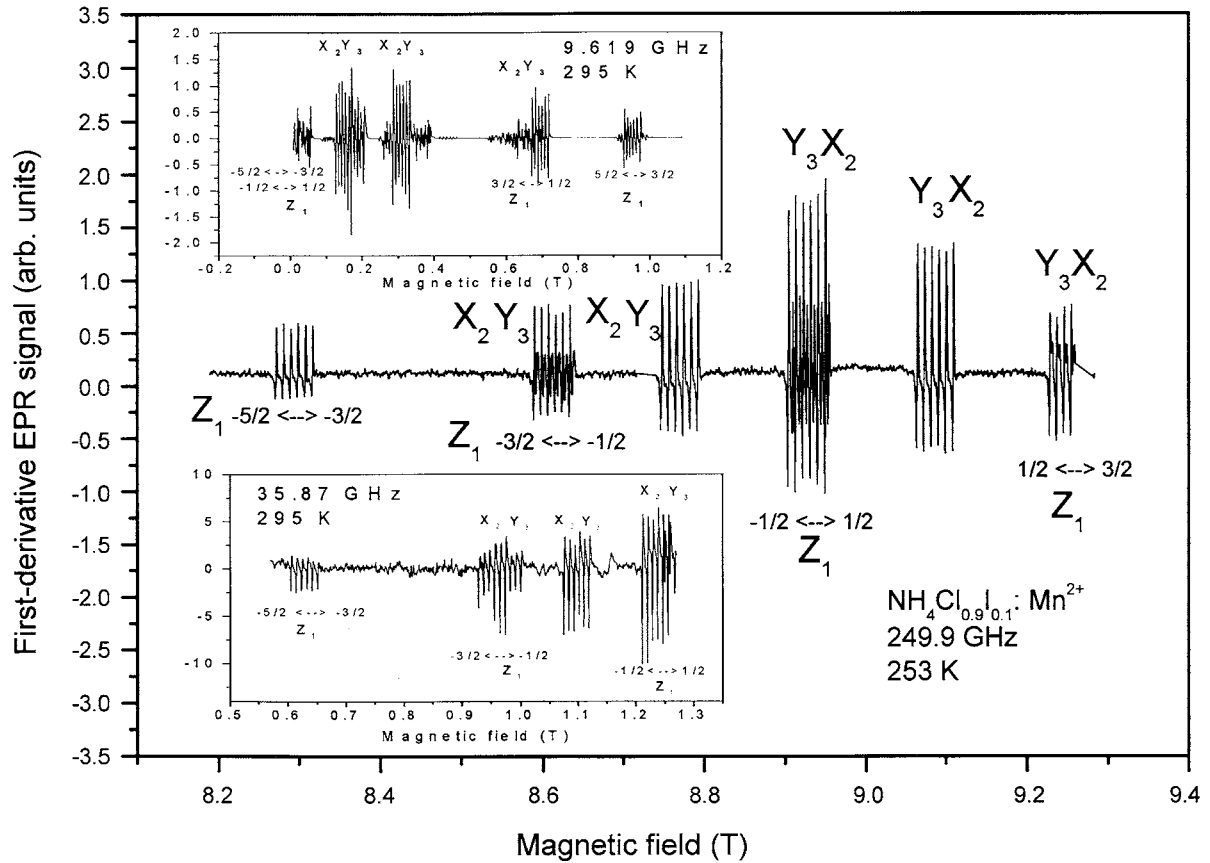


Fig. 2. Observed EPR spectra of the  $\text{Mn}^{2+}$  ions in the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal at 249.9 GHz (253 K) for  $B||Z_1||X_2||Y_3$  axes. (The subscripts refer to the three magnetically inequivalent ions.) The clearly resolved lines belonging to the three magnetically inequivalent ions are indicated by  $Z_1, X_2, Y_3$  for  $B||Z_1$  at 249.9 GHz. The fine-structure transitions corresponding to hyperfine sextets are indicated. The expected lines above 9.3 T are not observed at 249.9 GHz because 9.3 T is the upper limit of the magnetic field available at this frequency. It is seen that the FIR spectrum at 249.9 GHz provides considerable simplification of the spectrum allowing one to easily distinguish the EPR lines belonging to the three magnetically inequivalent ions. The insets show corresponding EPR spectra at X (9.619 GHz, 295 K) and Q (35.87 GHz, 295 K) bands.

$$\begin{aligned} \mathcal{H} = & \mu_B g [B_z S_z + B_x S_x + B_y S_y] + (1/3) b_2^0 O_2^0 \\ & + (1/60) b_4^0 O_4^0 + A(S_z I_z + S_x I_x + S_y I_y) \\ & + Q' [I_z^2 - I(I+1)/3], \end{aligned} \quad (3.1)$$

where the spin operators  $O_2^0 = [S_z^2 - S(S+1)/3]$ ,  $O_4^0 = [35S_z^4 - \{30S(S+1) - 25\}S_z^2 + 3S^2(S+1)^2 - 6S(S+1)]$ . In (3.1),  $S = 5/2$  is the electronic spin of the  $\text{Mn}^{2+}$  ion with  $S_z$  the  $Z$  component of the electronic spin operator, and  $I = 5/2$  is the nuclear spin of the  $^{55}\text{Mn}$  nucleus;  $b_2^0 (= D)$  and  $b_4^0$  are the ZFS parameters;  $Q'$  is the axial component of the nuclear quadrupole splitting tensor, and  $\mu_B$  is the Bohr magneton. The  $\mathbf{g}$  and the HF-structure tensor,  $\mathbf{A}$ , were here assumed to be isotropic consistent with the  $S$ -state nature of the  $\text{Mn}^{2+}$  ion.

The SHP were estimated as follows. First, the fine-structure (FS) parameters were evaluated separately at each frequency band using the least-squares/matrix diagonalization (LSFMD) procedure [24], fitting all the estimated FS EPR line positions,  $B_F(M)$ , at 9.62, 35.87, and 249.9 GHz at 295, 295, and 253 K, respectively, using Eq. (3.2) below. (Here  $M, m = \pm 1/2, \pm 3/2, \pm 5/2$

are the electronic and nuclear magnetic quantum numbers, respectively). The  $B_F(M)$  were estimated from,  $B_{HF}(M, m)$ , the hyperfine (HF) line positions, using the following relation [25]:

$$\begin{aligned} B_F(M) = & (3/4)[B_{HF}(M, 5/2) + B_{HF}(M, -5/2)] - (1/8) \\ & \times \{[B_{HF}(M, 3/2) + B_{HF}(M, -3/2)] \\ & + [B_{HF}(M, 1/2) + B_{HF}(M, -1/2)]\}. \end{aligned} \quad (3.2)$$

The angular variations of the  $\text{Mn}^{2+}$  FS line positions as well as the line positions calculated using the SH parameters listed in Table 1, obtained at 249.9 GHz, are shown in Fig. 4, which also includes those at 9.6 and 35.9 GHz as insets. The LSFMD procedure was then used to estimate the  $\text{Mn}^{2+}$  SH parameters by fitting simultaneously all the HF lines observed at X-, Q-, and FIR bands at 295, 295, and 253 K, respectively, assuming that there occurs no significant change in the SHP between 295 and 253 K. They are listed in Table 1. The absolute sign of the parameter  $b_2^0$  could not be determined from the present measurements due to lack of liquid-helium data. The minus sign has been used in accordance with that

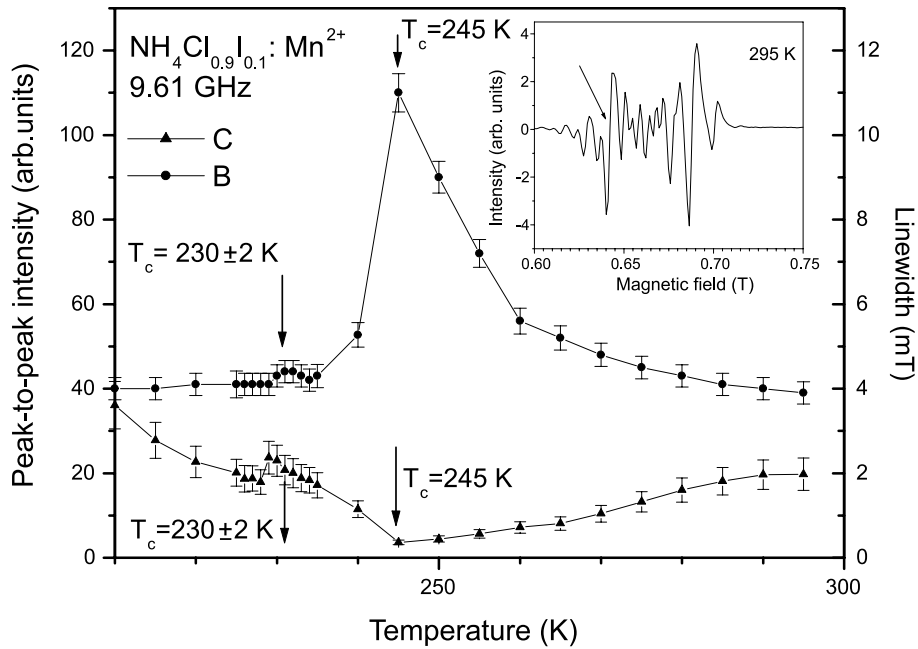


Fig. 3. Temperature variation of the first derivative peak-to-peak height and width of the hyperfine EPR lines belonging to the highest-field sextet at the orientation of  $B$  at  $60^\circ$  from the  $Z$ -axis in the  $(001)$  plane at 9.6 GHz. The solid circles indicate the observed values for the linewidth, while the triangles indicate the observed peak-to-peak height. An EPR spectrum at room temperature is also shown in the inset, with the arrow indicating the line used for the demonstration of occurrence of phase transition. The continuous lines connect data points as an aid to the eye.

Table 1

Estimated values of the  $\text{Mn}^{2+}$  spin-Hamiltonian parameters in  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal for one of the magnetically inequivalent ions

	X-band		Q-band		FIR-band	(X + Q + FIR)
	9.619 GHz	9.696 GHz	35.87 GHz	36.06 GHz	249.9 GHz	bands simultaneous fit
Temperature	295 K	125 K	295 K	77 K	253 K	295 K (253 K)
$n$	180	222	138	276	224	542
$g$	$2.0052 \pm 0.0002$	$1.9986 \pm 0.0002$	$2.0103 \pm 0.0001$	$2.0115 \pm 0.0001$	$1.9997 \pm 0.0001$	$1.9997 \pm 0.0001$
$b_2^0$ (GHz)	$-4.540 \pm 0.001$	$-4.637 \pm 0.001$	$-4.572 \pm 0.001$	$-4.780 \pm 0.001$	$-4.538 \pm 0.001$	$-4.563 \pm 0.001$
$b_4^0$ (GHz)	$0.014 \pm 0.001$	$0.001 \pm 0.001$	$0.014 \pm 0.001$	$0.010 \pm 0.001$	$0.009 \pm 0.001$	$0.019 \pm 0.001$
$A$ (GHz)	$-0.2438 \pm 0.0002$	$-0.2376 \pm 0.0002$	$-0.2547 \pm 0.0003$	$-0.2515 \pm 0.0003$	$-0.2489 \pm 0.0003$	$-0.2502 \pm 0.0003$
RMSL (GHz)	0.03	0.05	0.05	0.03	0.11	0.11

Due to their physical equivalence, the same SHP values are expected for the other two magnetically inequivalent  $\text{Mn}^{2+}$  ions. Here  $n$  is the number of hyperfine line positions fitted simultaneously in the least-squares procedure;  $\text{SMD}(\text{GHz}^2) = \sum_i (\Delta E_i - \nu_i)^2$ , where  $\Delta E_i$  is the calculated energy difference in GHz between the levels participating in resonance for the  $i$ th line position;  $\nu_i$  is the corresponding klystron frequency in GHz;  $h$  is Planck's constant; and  $\text{RMSL} = (\text{SMD}/n)^{1/2}$ . The value of  $Q$  was indeterminate within experimental error, and is therefore not listed here.

determined in [4] from the relative intensity of the  $\text{Mn}^{2+}$  EPR lines at 1.43 K in the  $\text{NH}_4\text{Cl}$  crystal. Since the LSFMD procedure yields the correct relative sign of all the parameters, the signs in Table 1 can then be considered as absolute. The absolute sign of the hyperfine interaction constant  $A$  has been determined to be negative from hyperfine-interaction data [26].

#### 4. Application of the superposition model: immediate environment of the $\text{Mn}^{2+}$ ion

The spin-Hamiltonian parameters for the  $\text{Mn}^{2+}$  ion in the mixed single crystal  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  can be interpreted in the context of the superposition model (SM)

[27] to better understand the immediate environment of the  $\text{Mn}^{2+}$  ion. In the superposition model the SHP are expressed as sums of contributions due to the nearest-neighbor ligand ions. When a monovalent ( $\text{NH}_4^+$ ) cation with the ionic radius of 1.43 Å [28] is replaced by a divalent  $\text{Mn}^{2+}$  cation with the ionic radius of 0.80 Å, charge-compensation occurs to preserve electrical neutrality resulting in the creation of a vacancy near the  $\text{Mn}^{2+}$  ion, associated with local distortions due to the difference in the impurity and host ion radii [4–6,12–15]. The  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal is assumed to have the SC structure, the same as that of  $\text{NH}_4\text{Cl}$ , taking into account the predominantly large proportion (90%) of  $\text{Cl}^-$  ions. In the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal, on average, 9 out of 10 anions lattice sites will be occupied by the  $\text{Cl}^-$  ion, while

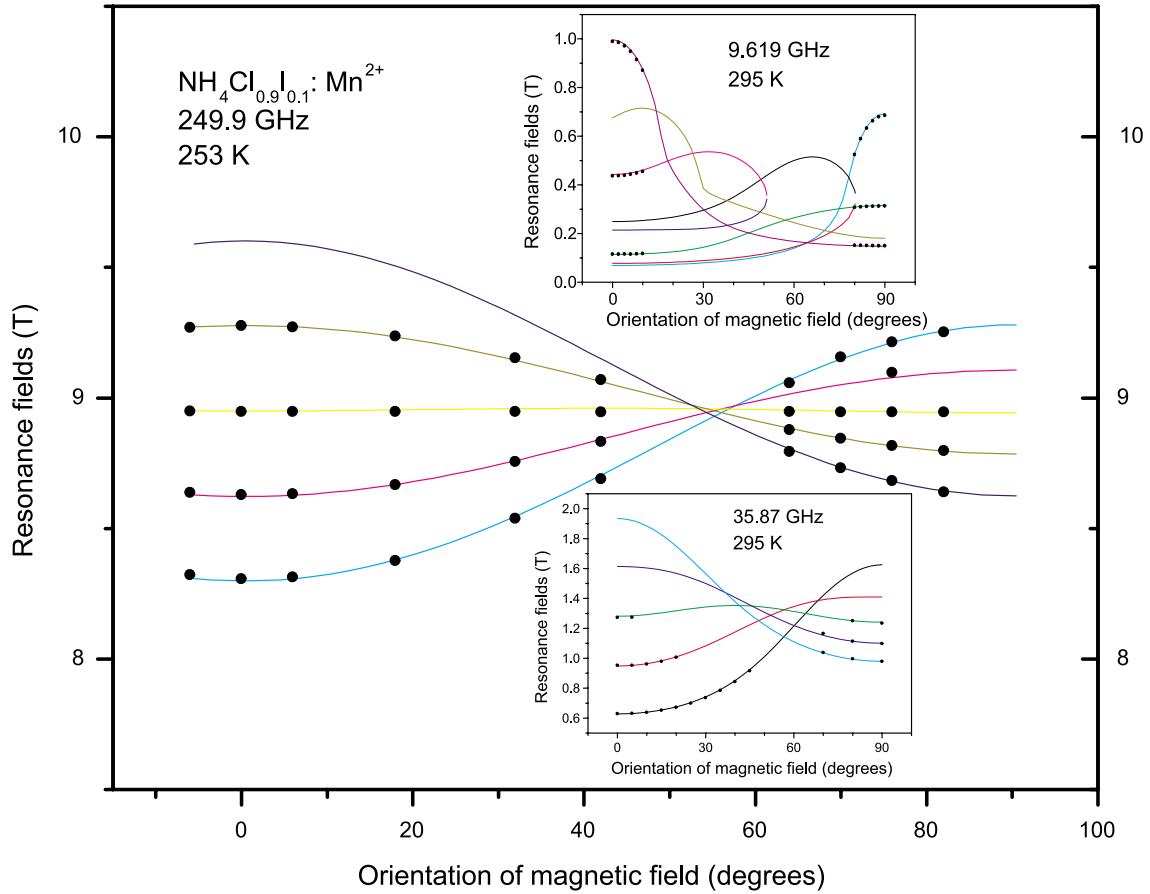


Fig. 4. Angular variation of the fine-structure EPR line positions for one of the three magnetically inequivalent  $\text{Mn}^{2+}$  ions in  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal at 249.9 GHz at 253 K as deduced from the experimentally observed hyperfine line positions using Eq. (3.2), and those calculated using the SHP listed in Table 1. Solid circles show experimentally observed line positions, while continuous lines show calculated ones. It is noted that due to upper limit on the magnetic field available at 249.9 GHz, EPR lines for  $B > 9.3$  T were not observed. The insets show corresponding angular variations at X (9.619 GHz, 295 K) and Q (35.87 GHz, 295 K) bands. The expected EPR lines at Q band for  $B > 1.3$  T are also not observed due to the upper limit on the available magnetic field value in the spectrometer.

the remaining one is occupied by the  $\text{I}^-$  ion for uniform doping.

For the axial symmetry case indicated here by the EPR spectra for each magnetically inequivalent  $\text{Mn}^{2+}$  ion only the parameters  $b_2^0$  and  $b_4^0$  are non-zero. These can be expressed, within the framework of the superposition model, as sums of the contributions from the various ligands  $i$  [27]:

$$b_2^0 = \sum_i \frac{1}{2}(3 \cos^2 \theta_i - 1) \bar{b}_2(R_0)(R_0/R_i)^{t_2}, \quad (4.1)$$

$$b_4^0 = \sum_i \frac{1}{8}(35 \cos^4 \theta_i - 30 \cos^2 \theta_i + 3) \bar{b}_4(R_0)(R_0/R_i)^{t_4}. \quad (4.2)$$

In (4.1), the  $\text{Mn}^{2+}$  cation is assumed to be at the origin (0, 0, 0) of a coordinate system located within the crystal, with the  $i$ th  $\text{Cl}^-$ , or  $\text{I}^-$ , ligand ion located at position  $(R_i, \theta_i, \phi_i)$  relative to this cation; here the variable  $R_i$  denotes the distance between the impurity cation

and the  $i$ th ligand ion.  $R_0$  is the reference ligand distance and  $t_n$  is a power law exponent. For the  $\text{Mn}^{2+}$  ion [27,29],  $t_2$  and  $t_4$  are usually assumed to be equal:  $7 \pm 1$ . For  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$ ,  $\theta_i = \pm 54.74^\circ$  for the eight ligand  $\text{Cl}^-$  or  $\text{I}^-$  ions which are situated at the vertices of a cube in the SC structure, with the  $\text{Mn}^{2+}$  ion situated at its center, and the  $Z$ -axis oriented along one of the crystallographic axes [1 0 0], [0 1 0], [0 0 1], as shown in Fig. 1 for this configuration. It is found from Eq. (4.1), since  $3 \cos^2 \theta = 1$  for  $\theta = \pm 54.74^\circ$ , that the parameter  $b_2^0 = 0$ , when the  $\text{Mn}^{2+}$  ion replaces an  $\text{NH}_4^+$  ion at its crystallographic position and no displacement of any ligand from its original position occurs. In order for this parameter to become large, and for the local site symmetry to become axial, as observed in this work, it is necessary that: (i) the  $\text{Mn}^{2+}$  ion be displaced sufficiently along a cubic axis from the  $\text{NH}_4^+$  position so that  $\theta_i$  is significantly different from  $54.74^\circ$ , (ii) a redistribution of ligand ions occurs to produce an axially symmetry crystal field at the  $\text{Mn}^{2+}$  ion, and (iii) the vacancies due

to charge-compensation occur at  $\text{NH}_4^+$  sites adjacent to an  $\text{Mn}^{2+}$  ion on the cubic axis on which the displacement of the  $\text{Mn}^{2+}$  ion takes place. There are thus six possible positions for these vacancies consistent with the presence of three magnetically inequivalent ions with their respective magnetic  $Z$ -axes oriented along the three crystallographic axes, each ion exhibiting an axially symmetric spectrum about its own  $Z$ -axis.

To explain the observed axial symmetry of the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal, as opposed to the tetragonal symmetry expected from the undisplaced positions of ligands, it is proposed here that the  $\text{Mn}^{2+}$  ion, in conjunction with the vacancy, causes a significant reorganization of its immediate environment such that it sees an axially symmetric crystal field at its site. The experimental value of  $b_2^0 = -4.56$  GHz estimated here is rather large for an inorganic crystal host [19]. Furthermore, almost the same values,  $b_2^0 = -4.515$  and  $-4.498$  GHz, were observed for the  $\text{Mn}^{2+}$  ion in  $\text{NH}_4\text{I}$  and  $\text{NH}_4\text{Cl}$  with FCC and SC structures, respectively [4,12]. This implies that substitution of a divalent  $\text{Mn}^{2+}$  ion for a monovalent  $\text{NH}_4^+$  ion in both the  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals, and thus in the mixed  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  crystal, results in a significant local rearrangement near the  $\text{Mn}^{2+}$  ion. These are almost the same for the two cubic structures SC and FCC of the  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals, respectively. Thus the  $\text{NH}_4^+$  ions play the dominant role in determining the spin-Hamiltonian parameters in  $\text{NH}_4\text{I}$ , and  $\text{NH}_4\text{Cl}$ , and the halide ions,  $\text{Cl}^-$  and  $\text{I}^-$ , contribute to the  $\text{Mn}^{2+}$  SHP only in a marginal manner.

## 5. Discussion and concluding remarks

The salient features of the EPR studies presented here are as follows:

(i) FIR EPR at 249.9 GHz provides a considerable simplification of the EPR spectrum making it quite easy to distinguish the three magnetically inequivalent  $\text{Mn}^{2+}$  ions, which is rather difficult at X (9.6 GHz) and Q (36 GHz) bands.

(ii) The symmetry of  $\text{Mn}^{2+}$  EPR spectra and the values of the SH parameters indicate that the  $\text{Mn}^{2+}$  ions are displaced from the  $\text{NH}_4^+$  positions along the three cubic axes accompanied by a vacancy at adjacent  $\text{NH}_4^+$  sites in the direction of the displacement for charge-compensation. As a consequence, the immediate environment around an  $\text{Mn}^{2+}$  ion in the  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  cubic crystal is changed considerably from that at an  $\text{NH}_4^+$  site, so that an axially symmetric crystal field is produced at its site. The same is true of the  $\text{Mn}^{2+}$ -doped  $\text{NH}_4\text{I}$  and  $\text{NH}_4\text{Cl}$  crystals [4–6,12–15]. As a consequence all the crystals,  $\text{NH}_4\text{Cl}$ ,  $\text{NH}_4\text{I}$ , and  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  are characterized by about the same values of the parameters  $b_2^0$  and  $b_4^0$  for the  $\text{Mn}^{2+}$  ion, with axial symmetry about its  $Z$ -axis.

(iii) Vacancies are created due to charge-compensation resulting from substitution of divalent  $\text{Mn}^{2+}$  ions for monovalent  $\text{NH}_4^+$  ions. These are situated at the next-neighbor sites to  $\text{Mn}^{2+}$  ions in the [100], [010], [001] crystallographic directions. This results in three magnetically inequivalent, but physically equivalent,  $\text{Mn}^{2+}$  ions in the mixed  $\text{NH}_4\text{Cl}_{0.9}\text{I}_{0.1}$  single crystal with the three magnetic  $Z$ -axes oriented along the cube edges.

(iv) Very accurate values of the SHP have here been estimated by fitting simultaneously all EPR line positions observed at X-, Q-, and FIR bands.

(v) The temperature variation of the  $\text{Mn}^{2+}$  EPR linewidth and peak-to-peak intensity of some of the highest-field lines in the range 120–300 K clearly indicate occurrence of  $\lambda$ -phase transitions at 245 and 230 K, corresponding to transitions observed in the pure  $\text{NH}_4\text{Cl}$  and  $\text{NH}_4\text{I}$  crystals.

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## References

- [1] A.G. Brenosa, F. Rodriguez, M. Moreno, *Ferroelectrics* 106 (1990) 187.
- [2] H. Abe, H. Shirai, *J. Phys. Soc. Jpn.* 15 (1960) 1711.
- [3] M.M. Zaripov, G.K. Chirkin, *Z. Struct. Khim.* 5 (1964) 36.
- [4] M.M. Zaripov, G.K. Chirkin, *Sov. Phys. Solid State* 7 (1966) 2391.
- [5] A. Forman, J.A. van Wyk, *J. Chem. Phys.* 44 (1966) 73.
- [6] A. Forman, J.A. van Wyk, *Can. J. Phys.* 45 (1967) 3381.
- [7] T.J. Seed, *J. Chem. Phys.* 41 (1964) 1486.
- [8] V. Lupei, A. Lupei, F. Domsa, *J. Magn. Reson.* 19 (1975) 337.
- [9] R. Bramley, S.J. Strach, *Chem. Phys. Lett.* 79 (1981) 183.
- [10] J.A. Kennewell, J.R. Pilbrow, J.H. Price, *Phys. Lett. A* 27 (1968) 228.
- [11] J.A. Van Wyk, *J. Magn. Reson.* 18 (1975) 235.
- [12] P. Chand, G.C. Upreti, *J. Chem. Phys.* 78 (1983) 5930.
- [13] P. Chand, G.C. Upreti, *J. Chem. Phys.* 81 (1984) 1650.
- [14] P. Chand, G.C. Upreti, S.K. Misra, M. Bartkowski, *J. Chem. Phys.* 82 (1985) 5307.
- [15] P. Chand, Ph.D. thesis. Electron paramagnetic resonance study of ammonium iodide single crystals doped with  $\text{Cu}^{2+}$ ,  $\text{Mn}^{2+}$ , and  $\text{VO}^{2+}$  submitted to Indian Institute of Technology (IIT), Kanpur, India, 1983 and the references cited in the thesis in this context.
- [16] S.K. Misra, in: C.P. Poole Jr., H.A. Farach (Eds.), *Handbook of Electron Spin Resonance*, vol. 2, Springer, New York, 1999, p. 85.
- [17] M.D. Sastry, Ph.D. thesis, I.I.T. Kanpur, India, 1967.
- [18] S.K. Misra, S.I. Andronenko, K.A. Earle, J.H. Freed, *Appl. Magn. Reson.* 21 (2001) 549.
- [19] S.K. Misra, in: A. Kawamori, Y. Yamauchi, H. Ohta (Eds.), *High-Frequency Single-Crystal EPR Application to Multifrequency Approach: Study of Metalloproteins*, EPR in the 21st

- Century, Elsevier Science, Amsterdam, 2002, pp. 731–740, Refereed Proceedings of the Asia Pacific EPR Society, 2001 conference, Kobe, Japan.
- [20] L. Vegard, *Z. Phys.* 5 (1921) 17.
- [21] H.A. Levy, S.W. Peterson, *J. Am. Chem. Soc.* 75 (1953) 1536.
- [22] W.B. Lynch, K.A. Earle, J.H. Freed, *Rev. Sci. Instrum.* 59 (1988) 1345.
- [23] S.K. Misra, J. Sun, *Magn. Reson. Rev.* 16 (1991) 157.
- [24] S.K. Misra, *J. Magn. Reson.* 23 (1976) 406.
- [25] S.K. Misra, *Physica B* 121 (1983) 193.
- [26] A. Steudel, in: *Hyperfine Interaction*, Academic Press, New York, 1976, p. 182.
- [27] D.J. Newman, *Adv. Phys.* 20 (1971) 197.
- [28] C. Kittel, *Introduction to Solid State Physics*, Wiley, New York, 1961.
- [29] D.J. Newman, W. Urban, *Adv. Phys.* 24 (1975) 793.