

## **Supporting Information**

### Local Ordering at Mobile Sites in Proteins from NMR Relaxation: the Role of Site Symmetry

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**Table S1. Relevant Part of the D<sub>2h</sub> Point Group Character Table.<sup>a</sup>**

	E	C <sub>2</sub> (z)	C <sub>2</sub> (y)	C <sub>2</sub> (x)	i	$\sigma(xy)$	$\sigma(xz)$	$\sigma(yz)$	linear	quadratic
A <sub>g</sub>	1	1	1	1	1	1	1	1		$x^2, y^2, z^2$
B <sub>1u</sub>	1	1	-1	-1	-1	-1	1	1		$z$
B <sub>2u</sub>	1	-1	1	-1	-1	1	-1	1		$y$
B <sub>3u</sub>	1	-1	-1	1	-1	1	1	-1		$x$

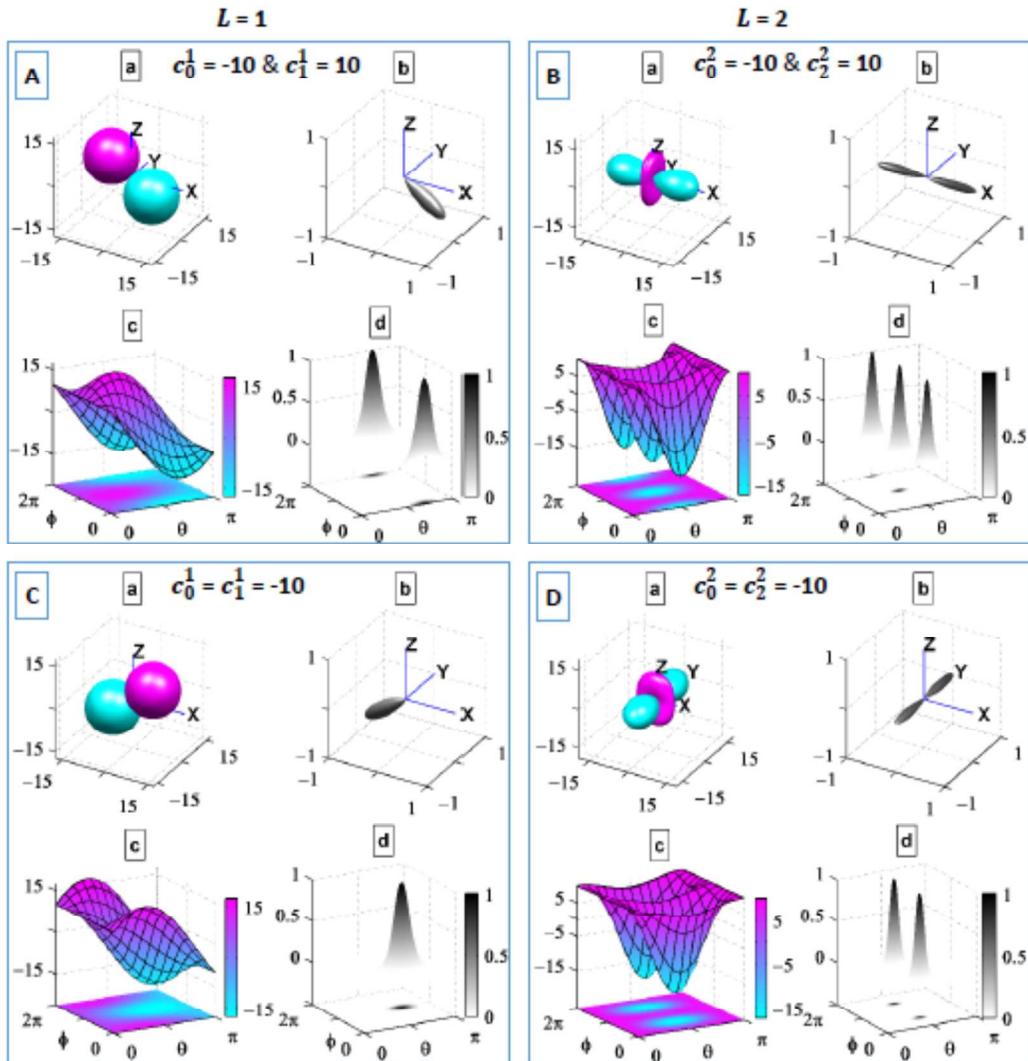
<sup>a</sup> The symmetry operations are E (identity), C<sub>2</sub> (two-fold rotation), i (inversion) and  $\sigma$  (reflection).  $x, y$  and  $z$  are the Cartesian coordinates.<sup>1</sup>

**Table S2. The Functions  $D_{00}^L(0, \theta, 0)$  for  $L = 1-4$ .<sup>2</sup>**

$L$	$D_{00}^L(0, \theta, 0)$
1	$\cos \theta$
2	$\left(\frac{1}{2}\right) [3 \cos^2 \theta - 1]$
3	$\left(\frac{1}{2}\right) \cos \theta [5 \cos^2 \theta - 3]$
4	$\left(\frac{1}{8}\right) \{[35 \cos^2 \theta - 30] \cos^2 \theta + 3\}$

**Table S3. Real Spherical Harmonics.<sup>1,3</sup>**

real spherical harmonics	corresponding atomic orbitals	definition in terms of Cartesian coordinates	D <sub>2h</sub> point group symmetry
$Y_{10}$	$p_z$	$\sqrt{\frac{3}{4\pi}} \cdot \frac{z}{r}$	B <sub>1u</sub>
$\sqrt{\frac{1}{2}} (Y_{1-1} - Y_{11})$	$p_x$	$\sqrt{\frac{3}{4\pi}} \cdot \frac{x}{r}$	B <sub>3u</sub>
$i \sqrt{\frac{1}{2}} (Y_{1-1} + Y_{11})$	$p_y$	$\sqrt{\frac{3}{4\pi}} \cdot \frac{y}{r}$	B <sub>2u</sub>
$Y_{20}$	$d_{z^2}$	$\frac{1}{4} \sqrt{\frac{5}{\pi}} \cdot \frac{2z^2 - x^2 - y^2}{r^2}$	A <sub>g</sub>
$\sqrt{\frac{1}{2}} (Y_{2-2} + Y_{22})$	$d_{x^2-y^2}$	$\frac{1}{4} \sqrt{\frac{15}{\pi}} \cdot \frac{x^2 - y^2}{r^2}$	A <sub>g</sub>



**Figure S1.** 4-panel representations of the scenarios  $L = 1, K = 0, 1$   $c_0^1 = -10$  and  $c_1^1 = 10$  (part A);  $L = 2, K = 0, 2$ ,  $c_0^2 = -10$   $c_2^2 = 10$  and (part B). 4-panel representations of the scenarios  $L = 1, K = 0, 1$   $c_0^1 = -10$  and  $c_1^1 = -10$  (part C);  $L = 2, K = 0, 2$ ,  $c_0^2 = -10$   $c_2^2 = -10$  and (part D). The potential,  $u$ , is represented in Cartesian coordinates in panels *a* and in spherical coordinates in panels *c*. The probability density function,  $\exp(-u)$ , is represented in Cartesian coordinates in panels *b* and in spherical coordinates in panels *d*. Further details are given in the text.

## References

1. *e-Chemical Portal,  $D_{2h}$  point group,* <http://www.webqc.org/printablesymmetrypointgroup-d2h.html>.
2. de Gennes, P. G.; Prost, J. *The Physics of Liquid Crystals*, Oxford Universiy Press, **1993**.
3. Zare, R. N. *Angular Momentum*, Wiley, Ch. 5, Application 13, p.226, **1988**.